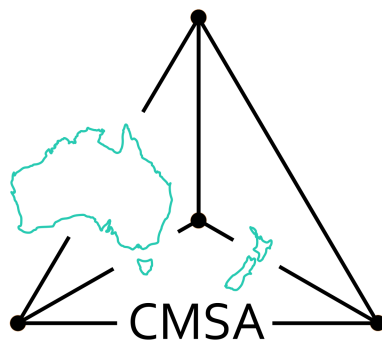


46TH AUSTRALASIAN COMBINATORICS CONFERENCE



The University of Queensland, 2–6 December, 2024



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Sara Davies

Barbara Maenhaut

Darryn Bryant

46acc.github.io/

Welcome!

Welcome to 46ACC and welcome to Brisbane. This is the seventh time a conference in this series has been hosted at the University of Queensland. The first hosting here (3rd ACCM) was 50 years ago in 1974. In addition to oversight and assistance provided by the Combinatorial Mathematics Society of Australasia, we gratefully acknowledge support from the Institute of Combinatorics and its Applications, and the School of Mathematics and Physics at the University of Queensland. We are delighted to have 70 registrants in attendance, and we wish you an enjoyable stay in Brisbane.

The organisers:

Sara Davies

Barbara Maenhaut

Darryn Bryant

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Schedule

Sunday

	Prentice 42 - outside room 216
16:00 – 18:00	Welcome reception and registration

Working Space

Room 67-146 (Level 1 of the Priestley Building) is available for use by conference attendees from 8am - 6pm Monday to Friday.

Monday

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Groups acting on trees and tree-like graphs

Florian Lehner

University of Auckland

The study of groups acting on infinite trees plays a foundational role in geometric group theory, and is instrumental in many other branches of mathematics such as algebraic topology (e.g. via the Seifert-van Kampen Theorem), and topological group theory (in particular, the study of totally disconnected, locally compact groups).

Bass-Serre theory is perhaps the most important tool for analysing group actions on trees. It relates group actions on trees to graphs of groups, allowing a description of the groups as iterated amalgamated free products and HNN extensions. Conversely, given a graph of groups, it allows us to construct a group action on a tree. Unfortunately, it is rather difficult to use this construction to obtain interesting new examples of groups acting on trees since the actions of vertex and edge stabilisers must satisfy strong compatibility conditions.

To overcome this issue, Reid and Smith recently introduced the theory of local action diagrams. This theory eliminates the need for compatibility conditions, but only allows for the construction of very specific groups. More precisely, it covers all groups satisfying Tits' property (P), in other words, groups for which there is no interaction between stabilisers of disjoint subtrees.

This talk consists of two parts. In the first part we give an overview of some key ideas in Bass-Serre theory and the theory of local action diagrams, highlighting the advantages and disadvantages of both approaches. In the second part, we introduce a new ("amalgamated") version of local action diagrams. The resulting theory can be thought of as "in between" Bass-Serre theory and the theory of local action diagrams in the sense that it allows us to model some interaction between stabilisers of disjoint subtrees, at the expense of re-introducing some weak compatibility conditions.

Although the motivation for much of the presented research comes from topological group theory, our methods are purely combinatorial. No background in topological group theory will be assumed.

The talk is based on joint work (at various stages of completion) with M. Chan, M. Hamann, C. Lindorfer, B. Mirafteb, R. Möller, T. Rühmann, and W. Woess.

Ramsey with purple edges

Anita Liebenau

UNSW Sydney

The classical Ramsey number $R(s, t)$ is the smallest number n such that every red-blue colouring of the edges of the complete graph on n vertices contains a complete red subgraph on s vertices, or a complete blue subgraph on t vertices. Since the introduction of Ramsey numbers by Erdős and Szekeres in 1935, the quest for finding Ramsey numbers has not only inspired powerful methods in graph theory and probabilistic combinatorics but also revealed profound connections to logic, computer science, and discrete geometry.

Motivated by a question of David Angell, we study a variant of Ramsey numbers where some edges are coloured both red and blue, or: purple. Specifically, we are interested in the largest number $g = g(s, t, n)$, for some s and t and $n < R(s, t)$, such that there exists a red-blue-purple colouring of the edges of K_n with g purple edges, without a red-purple K_s and without a blue-purple K_t . We determine g asymptotically for a large family of parameters. The talk will be introductory in nature. Joint work with Thomas Lesgourgues and Nye Taylor.

A hypergraph bipartite Turán problem

Jie Ma

University of Science and Technology of China

In this talk, we investigate the hypergraph Turán number $\text{ex}(n, K_{s,t}^{(r)})$. Here, $K_{s,t}^{(r)}$ denotes the r -uniform hypergraph with vertex set $(\cup_{i \in [t]} X_i) \cup Y$ and edge set $\{X_i \cup \{y\} : i \in [t], y \in Y\}$, where X_1, X_2, \dots, X_t are t pairwise disjoint sets of size $r - 1$ and Y is a set of size s disjoint from each X_i . This study was initially explored by Erdős and has since received substantial attention in research. Recent advancements by Bradač, Gishboliner, Janzer and Sudakov have greatly contributed to a better understanding of this problem. They proved that $\text{ex}(n, K_{s,t}^{(r)}) = O_{s,t}(n^{r-\frac{1}{s-1}})$ holds for any $r \geq 3$ and $s, t \geq 2$. They also provided constructions illustrating the tightness of this bound if $r \geq 4$ is even and $t \gg s \geq 2$. Furthermore, they proved that $\text{ex}(n, K_{s,t}^{(3)}) = O_{s,t}(n^{3-\frac{1}{s-1}-\epsilon_s})$ holds for $s \geq 3$ and some $\epsilon_s > 0$. Addressing this intriguing discrepancy between the behavior of this number for $r = 3$ and the even cases, Bradač et al. post a question of whether

$$\text{ex}(n, K_{s,t}^{(r)}) = O_{r,s,t}(n^{r-\frac{1}{s-1}-\epsilon}) \text{ holds for odd } r \geq 5 \text{ and any } s \geq 3.$$

We provide an affirmative answer to this question, utilizing novel techniques to identify regular and dense substructures. This result highlights a rare instance in hypergraph Turán problems where the solution depends on the parity of the uniformity. This is joint work with Tianchi Yang.

Heffter Spaces

Anita Pasotti

University of Brescia - Italy

A *half-set* of a group $(G, +)$ of odd order is a complete system of representatives for the set of all pairs of opposite elements of $G \setminus \{0\}$.

Let $(G, +)$ be an abelian group of order $2v + 1 \geq 7$. A (v, k) *Heffter system* on G is a partition \mathcal{P} of a half-set of G into zero-sum parts, called *blocks*, of size k . Two Heffter systems \mathcal{P} and \mathcal{Q} on the same half-set are *orthogonal* if every block of \mathcal{P} intersects every block of \mathcal{Q} in at most one element.

In 2015 Archdeacon [1] introduced the notion of a Heffter array as an interesting link between combinatorial designs and topological graph theory. In a few words a Heffter array is equivalent to a pair of orthogonal Heffter systems on a cyclic group. We refer to [6] for an extensive survey on these arrays, their variants and generalizations, and their connections to other topics.

In [2] we proposed the more general problem of constructing “many” mutually orthogonal Heffter systems, which led us to introduce a new combinatorial design, that we called a *Heffter space*. A $(v, k; r)$ Heffter space is a resolvable partial linear space of degree r whose point-set is a half-set of an abelian group G of order $2v + 1$ and whose blocks are zero-sum k -subsets of G . One of the motivations for studying Heffter spaces is that every $(v, k; r)$ Heffter space with suitable properties gives rise to r mutually orthogonal k -cycle systems of order $2v + 1$, a topic recently studied in [4, 5].

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Contributed talks

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Minimal simplicial degree d self-maps of

$$\mathbb{S}^{n-1} \times \mathbb{S}^1$$

Biplab Basak

Indian Institute of Technology Delhi

(Joint work with Anshu Agarwal and Sourav Sarkar)

In topology, the degree of a map between orientable manifolds is a crucial invariant that provides deep insights into the structural and geometric properties of the manifolds involved, as well as the relationships between them. Understanding how to construct maps of a given degree between manifolds has been the focus of extensive research, especially within the context of orientable topological spaces.

In this talk, we present a novel construction of degree d simplicial maps between orientable manifolds, specifically focusing on the product manifold $\mathbb{S}^{n-1} \times \mathbb{S}^1$. For each integer $d \in \mathbb{Z}$, we construct a simplicial map of degree d from a colored triangulation of $\mathbb{S}^{n-1} \times \mathbb{S}^1$ with $2(n+1) \max\{|d|, 1\}$ facets to the standard $2(n+1)$ -facet colored triangulation of $\mathbb{S}^{n-1} \times \mathbb{S}^1$. Our results demonstrate that these colored triangulations are minimal in the sense that they use the smallest possible number of facets necessary to support a degree d simplicial self-map of $\mathbb{S}^{n-1} \times \mathbb{S}^1$, where $n \geq 2$.

Furthermore, we extend our construction to provide a minimal degree d simplicial map from any closed orientable n -manifold to the standard n -sphere \mathbb{S}^n , for $n \geq 1$. These constructions not only shed light on the interplay between combinatorial and topological properties in the context of colored triangulations but also offer new tools for the study of simplicial maps and manifold topology.

Detachable pairs in 3-connected simple graphs and 3-connected matroids

Nick Brettell

Victoria University of Wellington

(Joint work with Charles Semple and Gerry Toft)

Tutte (1961) proved that a simple 3-connected graph G has an edge e such that either the deletion or contraction of e from G results in a graph that remains simple and 3-connected, unless G is a wheel. What if we instead ask for a pair of edges such that deleting both or contracting both retains simplicity and 3-connectedness? We call a pair of edges with this property *detachable*. In recent joint work with Gerry Toft and Charles Semple, building on work of Alan Williams (2014), we characterised the simple 3-connected graphs with no detachable pairs. In fact, we obtain this as a corollary of a more general result regarding detachable pairs in 3-connected matroids. In this talk, I will discuss this result, the motivation behind this work, and some potential applications.

Different ways of constructing infinite families of group divisible designs with two group sizes

Yudhistira Andersen Bunjamin

UNSW Sydney

(Joint work with R. Julian R. Abel, Thomas Britz, Diana Combe and Changyuan Wang)

A k -GDD, or group divisible design with block size k , is a triple (X, G, \mathcal{B}) where X is a set of points, G is a partition of X into subsets (called groups) and \mathcal{B} is a collection of k -element subsets of X (called blocks) such that any two points from distinct groups appear together in exactly one block and no two distinct points from any group appear together in any block. There are a number of known necessary conditions for the existence of a GDD. However, these conditions are not sufficient.

Over the past five years, we have constructed infinite families of 3-GDDs and 4-GDDs with only two group sizes for several pairs of group sizes. For each of these pairs of group sizes, the work usually requires piecing together several recursive constructions for smaller infinite families of k -GDDs. More recent work focused on 4-GDDs with only groups of size 4 and 10. This family of 4-GDDs was constructed quite differently from those that were constructed in the past.

In this talk, we will compare the different ways in which these constructions of smaller families have been pieces together to obtain constructions for the much larger infinite families. We will discuss the insights on the advantages and disadvantages these different methods that have been gained through the recent work on 4-GDDs with groups of size 4 and 10.

Joint work with R. Julian R. Abel, Thomas Britz, Diana Combe and Changyuan Wang

S -Arc-Transitivity of Vertex-Transitive Digraphs

Lei Chen*

University of Western Australia

The investigation of s -arc-transitivity can be dated back to 1947. Tutte [4] studied cubic graphs and showed that a cubic graph can be at most 5-arc-transitive. A more general result for s -arc-transitivity of graphs was obtained by Weiss [5] and it turns out that finite undirected graphs of valency at least 3 that are not cycles can be at most 7-arc-transitive. In stark contrast with the situation in undirected graphs, Praeger [3] showed that for each s and d there are infinitely many finite s -arc-transitive digraphs of valency d that are not $(s + 1)$ -arc-transitive.

However, once we add the condition of primitivity the situation gets quite different. Since the lack of evidence of existence of vertex-primitive 2-arc-transitive digraphs, Praeger [3] asked if there exists any vertex-primitive 2-arc-transitive digraph. The question was then answered in [1] and [2] by constructing infinite families of G -vertex-primitive $(G, 2)$ -arc-transitive digraphs such that G is AS and SD types, respectively. In [2] Giudici and Xia then asked for a G -vertex-primitive (G, s) -arc-transitive digraph that is not a directed cycle, what is the upper bound on s . A reasonable conjecture is that $s \leq 2$. At the same time, Giudici and Xia [2] showed that to answer that question it suffices for us to consider the case when G is almost simple.

In this talk, I will introduce the current progress of the study of the s -arc-transitivity of vertex-primitive digraphs of various almost simple groups. Indeed, all of the studied almost simple groups follow the conjecture that $s \leq 2$. Moreover, I will also discuss a bit about the s -arc-transitive vertex-quasiprimitive digraphs and show that for vertex-quasiprimitive digraphs, s can also be unbounded.

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On the Critical Problem for codes over $\mathbb{Z}/q\mathbb{Z}$

Koji Imamura

Kumamoto University

(Joint work with Norihiro Nakashima and Takuya Saito)

The *Critical Problem* posed by H. Crapo and G.-C. Rota in 1970 is one of the most significant problems in matroid theory. Let \mathbb{F}_q be a finite field of q elements. For any subset $S \subseteq \mathbb{F}_q^k$, the *critical exponent* of S is defined as follows:

$$c(S; q) := k - \max\{\dim D : D \leq \mathbb{F}_q^k \text{ and } D \cap S = \emptyset\}.$$

Then the problem is to find the critical exponent for a given subset S .

They also proved the *Critical Theorem*, which provides the matroid-theoretic approach to the Critical Problem. Let $p(M; \lambda)$ denote the characteristic polynomial of a matroid M and let M/X denote the contraction of M by $X \subseteq E$. Then the theorem is described as follows.

Theorem Let C be a k -dimensional subspace of \mathbb{F}_q^n and set $E := \{1, \dots, n\}$. For any $X \subseteq E$ and any $\ell \in \mathbb{Z}^+$, the number of ordered ℓ -tuples $(\mathbf{v}_1, \dots, \mathbf{v}_\ell)$ of integers of vectors in C with $\text{supp}(\mathbf{v}_1) \cup \dots \cup \text{supp}(\mathbf{v}_\ell) = X$ is $p(M_C/(E - X); q^\ell)$, where $\text{supp}(\mathbf{v}) = \{i \in E \mid v_i \neq 0\}$ for $\mathbf{v} = (v_1, \dots, v_n) \in \mathbb{F}_q^n$.

In this talk, we examine the Critical Problem for codes over the ring of integers modulo $q \in \mathbb{Z}^+$. For the purpose, we consider the theory of characteristic quasi-polynomial introduced by H. Kamiya, A. Takemura, and H. Terao in 2008. As an application, we study the weight enumerator of codes over $\mathbb{Z}/q\mathbb{Z}$.

Degree-based function index of trees, unicyclic graphs and bicyclic graphs with given bipartition

Pawaton Kaemawichanurat

King Mongkut's University of Technology Thonburi

(Joint work with Tomas Vetrik)

We investigate the degree-based function index $I_f(G) = \sum_{vw \in E(G)} f(d_G(v), d_G(w))$ of a graph G , where $E(G)$ is the set of edges of G , $d_G(v)$ and $d_G(w)$ are the degrees of vertices v and w in G , respectively, and f is a symmetric function of two variables which satisfies some conditions. We obtain sharp upper bounds on I_f for trees, unicyclic graphs and bicyclic graphs with given bipartition. Then, among trees and unicyclic graphs with given bipartition, we present graphs with the largest values of the general reduced second Zagreb index $GRM_a(G) = \sum_{vw \in E(G)} (d_G(v) + a)(d_G(w) + a)$ for $a > -1$, general Randić index $R_a(G) = \sum_{vw \in E(G)} [d_G(v)d_G(w)]^a$ and first general Gourava index $FGO_a(G) = \sum_{vw \in E(G)} [d_G(v)d_G(w) + d_G(v) + d_G(w)]^a$ for $a \geq 1$, general Sombor index $SO_{a,b}(G) = \sum_{vw \in E(G)} ([d_G(v)]^a + [d_G(w)]^a)^b$, generalized Zagreb index $GZ_{a,b}(G) = \sum_{vw \in E(G)} ([d_G(v)]^a [d_G(w)]^b + [d_G(v)]^b [d_G(w)]^a)$ and one other general index $M_{a,b}(G) = \sum_{vw \in E(G)} [d_G(v)d_G(w)]^a [d_G(v) + d_G(w)]^b$ for $a \geq 1$ and $b \geq 1$.

On Minimising the Number of Subsets and Supersets of a Family of Sets

Adam Mammoliti

UNSW Sydney

(Joint work with Daniel Horsley and Adam Gowty)

Let \mathcal{F} be a family of k -subsets of $[n]$. The lower shadow of \mathcal{F} is the set of all $(k - 1)$ -subsets of $[n]$ that are a subset of at least one member of \mathcal{F} and the upper shadow of \mathcal{F} is the set of all $(k + 1)$ -subsets of $[n]$ that are a superset of at least one member of \mathcal{F} . The Kruskal-Katona Theorem states that over all k -uniform families \mathcal{F} of subsets of $[n]$ with $|\mathcal{F}| = m$ the minimum size of the lower shadow of \mathcal{F} is that of the lower shadow of the first m k -subsets of $[n]$ in the colexicographical order. An analogous result is true if we instead minimise the size of the upper shadow of \mathcal{F} .

In this talk I present a generalisation of the Kruskal-Katona Theorem where the sets in the family \mathcal{F} need not be the same size and we consider minimising the size of \mathcal{F}^\updownarrow , the set of all subsets of $[n]$ that are either a subset or a superset of at least one member of \mathcal{F} , over all families $\mathcal{F} \subseteq 2^{[n]}$ with m members. I present a recursive formula for the minimum size of \mathcal{F}^\updownarrow for any n and $m \leq 2^n$. I also present a relative simple lower bound for the minimum size of $|\mathcal{F}^\updownarrow|$, namely it is true that $|\mathcal{F}^\updownarrow| \geq \sqrt{2^{n+2m}} - m$ where $\mathcal{F} \subseteq 2^{[n]}$ has $m \leq 2^n$ members. This bound is tight when it is an integer and is asymptotically correct as $n \rightarrow \infty$ with $m = \omega(1)$.

This is based on joint work with Daniel Horsley and Adam Gowty.

Marginal Analysis on Finite Sets

Ian Roberts

Charles Darwin University

An overview of a new mathematical approach is provided. The approach is called *Marginal Analysis* and it is applicable to a range of problems involving ordered collections of sets. The approach simplifies the analysis of some difficult contemporary problems and provides insight and solutions to a range of new or unsolved problems. These problems include the analysis of functions defined on collections of sets such as the Kruskal-Katona function and the Lubell function, and on various types of antichains and associated functions in the Boolean Lattice.

Marginal Analysis can be considered as a form of Discrete Calculus. On the surface, it is simple in concepts and requires a small mathematical tool-box, but one has to be discerning in the choice and blending of the parts. An overview of the approach will be described in a visual and non-technical form. Researchers in other areas may find some ideas and results of interest to them, and an opening into potential new work.

Marginal analysis uses the language of sets but the results can be applied to Hypergraphs, Graphs, Projective Geometry, Coding Theory, and Combinatorial Design. Antichains and the Kruskal-Katona function are core concerns, and thus the talk informs the study of independent sets, blocking sets, vertex covers, intersecting set systems, combinatorial designs, and more.

Useful background ideas and knowledge include antichains, the Kruskal-Katona Theorem and the associated squashed (or colex) order, and the BLYM (or LYM) inequality.

An Upper Bound Theorem for Homology 4-Manifolds

*Sourav Sarkar**

Indian Institute of Technology Delhi

(Joint work with Biplab Basak)

The g -vector of a simplicial complex contains significant information about the combinatorial and topological structure of the complex. Several classification results concerning the structure of normal pseudomanifolds and homology manifolds have been established in relation to the value of g_2 , the third component of the g -vector. It is known that when $g_2 = 0$, all normal pseudomanifolds of dimensions at least three are stacked spheres. Walkup proved that a homology 3-manifold with $g_2 \leq 9$ is a triangulated sphere. We demonstrate that homology 4-manifolds with $g_2 \leq 5$ are triangulated spheres and are derived from triangulated 4-spheres with $g_2 \leq 2$ by a series of connected sum, bistellar 1- and 2-moves, edge contraction, edge expansion, and edge flipping operations. Furthermore, we establish that this inequality is optimally attainable, i.e., it cannot be extended to $g_2 = 6$.

Characterization of Strongly Graceful Unicyclic Graphs

I Nengah Suparta

Mathematics Department, Ganesha University of Education

(Joint work with M. Bača, M. Demange, A. Semaničová-Feňovčíková, N.L.D. Sintuari)

A graph $G := G(V, E)$ we mean as a system which consists of a finite non-empty set V of vertices and a possibly empty set E of 2-element subsets of V called edges. For the sake of convenience we write uv for 2-element subset $\{u, v\}$, $u, v \in V$. The cardinality of V , $|V|$, and the cardinality of E , $|E|$, are called order and size of G , respectively. Let f be an injective function from the vertex set V into the set $\{0, 1, \dots, |E|\}$. If the set

$$\{|f(u) - f(v)| : uv \in E\} = \{1, 2, \dots, |E|\},$$

then f is called *graceful labeling* for G , and the graph G is called *graceful*. A *matching* in G is a non empty subset M of E such that any two elements of M are not adjacent in G . The matching M is called *perfect* if every vertex of G is incident with an element of M . In this case, the graph G is called with *perfect matching*. Let G be a graceful graph with graceful labeling f and some perfect matching M . If in addition, we also have that $f(u) + f(v) = |E|$ for every $uv \in M$, then f is called *strongly graceful labeling* for G , and the graph G is called *strongly graceful*. In this talk we characterize unicyclic graphs as strongly graceful graphs.

Lattice Paths and Order-Preserving Transformations of a Finite Chain

Abdullahi Umar

Khalifa University

(Joint work with A. Laradji)

Let \mathcal{PO}_n be the monoid of order-preserving partial transformations on $[n] = \{1, 2, \dots, n\}$. It is known that there exist bijections between \mathcal{PO}_n and its subsemigroups with certain lattice paths that start from $(0, 0)$ and end at $(n - 1, n - 1)$ in the Cartesian plane (Laradji and Umar, 2016). In this talk we are going to discuss several consequences of these bijections.



On covering radii of rank metric codes

*Takatomo Yamasaki**

Kumamoto University

(Joint work with Keisuke Shiromoto and Koji Imamura)

In classical coding theory, a linear code is a k -dimensional subspace C of \mathbb{F}_q^n . The Hamming distance between $x = (x_1, \dots, x_n)$ and $y = (y_1, \dots, y_n)$ in \mathbb{F}_q^n is defined by $d_H(x, y) := |\{i \mid x_i \neq y_i\}|$. Then, the *covering radius* $\rho(C)$ of a linear code C is defined as follows:

$$\rho(C) := \max_{x \in \mathbb{F}_q^n} \min_{c \in C} d_H(x, c).$$

The covering radius is one of the important parameters in a linear code for understanding the decoding and the error-detecting capabilities of the code. The following relationship between the covering radius and the weight distributions was introduced by Delsarte in 1973:

Theorem (Delsarte bound) *Let $A_i(C^\perp)$ be the number of vectors in the dual space C^\perp of a linear code C whose Hamming weight is i . Then $\rho(C) \leq s$, where s is the number of $i \in \{1, \dots, n\}$ such that $A_i(C^\perp) \neq 0$.*

In this talk, we study the Delsarte bound for a *Delsarte rank metric code*, a subspace of the \mathbb{F}_q -linear space consisting of the $n \times m$ matrices. The bound has already been proved in terms of algebraic graph theory. However, we provide an alternative proof for the bound from a coding-theoretic perspective by introducing coset structure in rank metric codes. As an application of our coset structure, we propose a construction of *maximum rank distance* (MRD) codes from almost MRD codes.

On the minimum length of linear codes

Keita Yasufuku*

Osaka Metropolitan University

(Joint work with Tatsuya Maruta)

A q -ary linear code of length n with dimension k (an $[n, k]_q$ code) is a k -dimensional subspace of the n -dimensional row vector space over the field of q elements. An $[n, k]_q$ code with minimum distance d is called an $[n, k, d]_q$ code.

We consider the problem to find optimal $[n, k, d]_q$ codes. This problem in coding theory is that of optimizing one of the parameters length n , dimension k , minimum distance d for given the other two which is referred to as the “optimal linear code problem”.

Also, it is known that the Griesmer bound is attained for all sufficiently large d for fixed q and k .

We tackle the problem to find $D_{q,k}$, the largest d such that the Griesmer bound is not attained for fixed k and q . This problem is solved when q is much larger than k .

In this presentation, we give a conjecture of $D_{q,k}$ and show that our conjecture on $D_{q,k}$ is valid for $q + 1 \leq k \leq 8$ with $4 \leq q \leq 7$.

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List of participants

Name	Affiliation	email address
Maliheh Alaei	The University of Queensland	m.alaeitazehkand@uq.edu.au
Jack Allsop	Monash University	jack.allsop@monash.edu
Maram Alqarni	The University of Queensland	maram.alqarni@student.uq.edu.au
Dickson Annor	La Trobe University	d.annor@latrobe.edu.au
Biplab Basak	Indian Institute of Technology Delhi	biplab@iitd.ac.in
Abdul Basit	Monash University	abdul.basit@monash.edu
Nick Brettell	Victoria University of Wellington	nick.brettell@vuw.ac.nz
Darryn Bryant	The University of Queensland	db@maths.uq.edu.au
Yudhistira Andersen Bunjamin	UNSW Sydney	yudhi@unsw.edu.au
Lei Chen	University of Western Australia	lei.chen@uwa.edu.au
Katie Clinch	UNSW Sydney	k.clinch@unsw.edu.au
Marston Conder	University of Auckland	m.conder@auckland.ac.nz
Sara Davies	The University of Queensland	sara.davies@uq.edu.au
Ajani De Vas Gunasekara	The University of Notre Dame, Australia	ajani.de.vas.gunasekara@nd.edu.au
Alice Devillers	University of Western Australia	alice.devillers@uwa.edu.au
Marc Distel	Monash University	Marc.Distel@monash.edu
Diane Donovan	The University of Queensland	dmd@maths.uq.edu.au
Christopher Duffy	University of Melbourne	christopher.duffy@unimelb.edu.au
Muhammad Talha Farooq	Macquarie University Sydney New South Wales	muhammadtalharao1@gmail.com
Graham Farr	Monash University	Graham.Farr@monash.edu
Afsane Ghafari Baghestani	Monash University	afsane.ghafaribaghestani@monash.edu
Gary Greaves	Nanyang Technological University, Singapore	grwgrvs@gmail.com
Raju Kumar Gupta	Indian Institute of Technology Delhi	rajugupta6174@gmail.com
Hao Chuien Hang	National Institute of Education, Singapore	hanghc@hotmail.com
Sakander Hayat	Universiti Brunei Darussalam	sakander.hayat@ubd.edu.bn
Kevin Hendrey	Monash University	kevin.hendrey1@monash.edu
Hung Hoang	TU Wien	phoang@ac.tuwien.ac.at
Daniel Horsley	Monash University	daniel.horsley@monash.edu
Koji Imamura	Kumamoto University	k-imamura@kumamoto-u.ac.jp
Mikhail Isaev	UNSW	isaev.m.i@gmail.com
Pawaton Kaemawichanurat	King Mongkut's University of Technology	pawaton.kae@kmutt.ac.th
Tara Kemp	The University of Queensland	t.kemp@uq.net.au
Jonathan Klawitter	University of Auckland	jonathan.klawitter@auckland.ac.nz
Sarah Lawson	The University of Queensland	sarah.lawson@uq.edu.au
Melissa Lee	Monash University	melissa.lee@monash.edu
James Lefevre	The University of Queensland	j.lefevre@uq.edu.au
Florian Lehner	University of Auckland	florian.lehner@auckland.ac.nz
Paul Leopardi	ACCESS-NRI	paul.leopardi@anu.edu.au
Thomas Lesgourgues	University of Waterloo	tlesgourgues@uwaterloo.ca
Anita Liebenau	UNSW Sydney	a.liebenau@unsw.edu.au
Jie Ma	University of Science and Technology of China	jiema@ustc.edu.cn
Barbara Maenhaut	The University of Queensland	bmm@maths.uq.edu.au
Adam Mammoliti	UNSW Sydney	adam.mammoliti@outlook.com.au
Sam Mattheus	Vrije Universiteit Brussel	sam.mattheus@vub.be
Brendan McKay	Australian National University	brendan.mckay@anu.edu.au
Đorđe Mitrović	University of Auckland	dmit755@aucklanduni.ac.nz
Jack Neubecker	The University of Queensland	j.neubecker@uq.edu.au
Semin Oh	Kyungpook National University	semin@knu.ac.kr
Anita Pasotti	Università degli Studi di Brescia	anita.pasotti@unibs.it
Tomasz Popiel	Monash University	tomasz.popiel@monash.edu
Cheryl Praeger	University of Western Australia	cheryl.praeger@uwa.edu.au
M.Tariq Rahim	Abbottabad University of Science and Technology Pakistan	tariqsms@gmail.com
Guang Rao	National University of Singapore	generalrao@hotmail.com
Ian Roberts	CDU	ian.roberts@cdu.edu.au
Sourav Sarkar	Indian Institute of Technology Delhi	sarkarsourav610@gmail.com

Ian Seong	University of Wisconsin-Madison	iseong@wisc.edu
Shiksha Shiksha	La Trobe University, Bendigo Campus, Bendigo	22044854@students.ltu.edu.au
Matthew Slattery-Holmes	University of Otago	slama077@student.otago.ac.nz
I Nengah Suparta	Ganesha University of Education	nengah.suparta@undiksha.ac.id
Nye Taylor	UNSW	nyem.taylor@gmail.com
Brhane Gebremichel Tnsau	University of Science and Technology of China	brhane@ustc.edu.cn
Abdullahi Umar	Khalifa University	abdullahi.umar@ku.ac.ae
Geertrui Van de Voorde	University of Canterbury	geertrui.vandevoorde@canterbury.ac.nz
Lander Verlinde	University of Auckland	lver263@aucklanduni.ac.nz
Ian Wanless	Monash University	ian.wanless@monash.edu
David Wood	Monash University	david.wood@monash.edu
Nick Wormald	Monash University	nick.wormald@monash.edu
Takatomo Yamasaki	Kumamoto University	230d8568@st.kumamoto-u.ac.jp
Keita Yasufuku	Osaka Metropolitan University	keita0125sve@icloud.com
Zhaorui Zhang	University of Queensland	zhaorui.zhang@uq.net.au